

OPAQUE is NOT Magic

**Steve “Sc00bz” Thomas**

# What is a PAKE?



# PAKEs

- Password authentication
- Encrypted tunnels
- Sending files
  - <https://github.com/magic-wormhole>
- Fighting phone spoofing
  - <https://commsrisk.com/?p=35506>



# How PAKEs Work

$a = \text{random}()$

$A = a * G$

# Hide the Ephemeral Keys

$a = \text{random}()$

$A = a * G + P$

# Hide the Generator

`a = random()`

`A = a*P`

# Myth #1

- “Zero knowledge” means the server doesn't have a password hash

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- “Zero knowledge” means the server doesn't have a password hash
- “Augmented PAKE for authentication: we recommend the usage of OPAQUE to avoid targeted dictionary attacks on user passwords by [the company].”

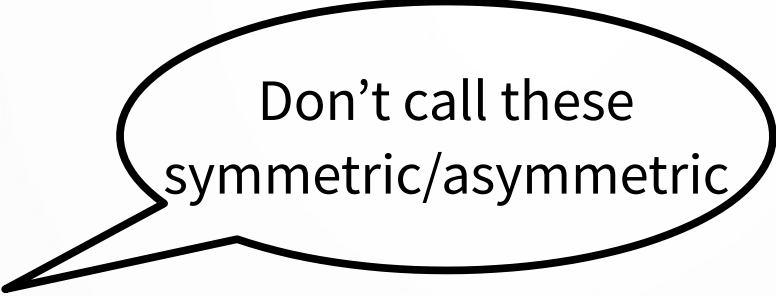


# Myth #2

- OPAQUE is an augmented PAKE

# Types of PAKEs

- Balanced
  - Peer-to-Peer
- Augmented (aPAKE)
  - Client-Server



Don't call these  
symmetric/asymmetric

# Types of PAKEs

- Balanced
  - Peer-to-Peer
- Augmented (aPAKE)
  - Client-Server
- Doubly Augmented
  - Client-Server/Device-Server
- Identity
  - IoT



# Myth #3

- OPAQUE should be used for TLS because other PAKEs need to send the user name

# OPRF

C:  $P = \text{hashToCurve}(\text{pw}, \text{id}, \dots)$

C:  $r = \text{random}()$

C:  $R = r * P$

C → S:  $\text{id}, R$

S:  $\text{salt} = \text{dbLookup}(\text{id})$

S:  $R' = \text{salt} * R$

C ← S:  $R'$

C:  $\text{BlindSalt} = (1/r) * R'$

$\text{BlindSalt} == (1/r) * r * \text{salt} * P == \text{salt} * P$



# Myth #4

- OPAQUE is the only PAKE that can prevent precomputation attacks

# Myth #5

- Adding an OPRF to other PAKEs makes them much slower than OPAQUE

# Costs

## OPAQUE-3DH

C: fHI\*\*ii ff\*\*\*ix

S: f\*i ff\*\*\*x

\*: Scalar point multiply

x: Scalar base point multiply

H: Hash to curve

## BS-SPEKE

C: fHI\*\*ii f\*\*\*xiH

S: f\*i ff\*\*\*i

i: Field invert

I: Scalar invert

f: From bytes

# Costs

OPAQUE-3DH

C: fHI\*\*ii ff\*\*\*iX

S: f\*i ff\*\*\*X

\*: Scalar point multiply

x: Scalar base point multiply

H: Hash to curve

(strong) AuCPace

C: fHI\*\*ii ff\*\*\*iiH

S: f\*i ff\*\*\*XiiH

i: Field invert

I: Scalar invert

f: From bytes

# Costs

## OPAQUE-3DH

C: fHI\*\*ii ff\*\*\*ix

S: f\*i ff\*\*\*x

\*: Scalar point multiply

x: Scalar base point multiply

H: Hash to curve

## Double BS-SPEKE

C: fHI\*\*ii f\*\*\*xii\*H

S: f\*i ff\*\*\*i

i: Field invert

I: Scalar invert

f: From bytes



# Costs

OPAQUE-3DH

C: fHI\*\*ii ff\*\*\*ix

S: f\*i ff\*\*\*x

\*: Scalar point multiply

x: Scalar base point multiply

H: Hash to curve

OPAQUE-Noise-KN-No-AEAD

C: fHI\*\*ii f\*\*ixx

S: f\*i ff\*\*\*x

i: Field invert

I: Scalar invert

f: From bytes

# PAKE Properties

- Fragile
- Quantum Annoying

# Quantum Annoying

- “It is noted in [BM92] that if we assume that a discrete log pre-computation has been made for the modulus, a password attack must also compute the specific log for each entry in the password dictionary (until a match is found).”
  - SPEKE paper 1996
- “With EKE, the password  $P$  is used to superencrypt such values; it is not possible to essay a discrete logarithm calculation except for all possible guesses of  $P$ .”
  - EKE paper 1992

# Myth #6

- OPAQUE is the only one that can be made post quantum

# Myth #7

- If you have an HSM that does Curve25519 but not Ristretto255, then you can't use Ristretto255



# Myth #8

- You can't inverse a clamped scalar while preserving the clamp

# Clamp

ClampedScalar =

data % 2\*\*254

+ 2\*\*254

- data % 8

min = 0x4000

max = 0x7fff8

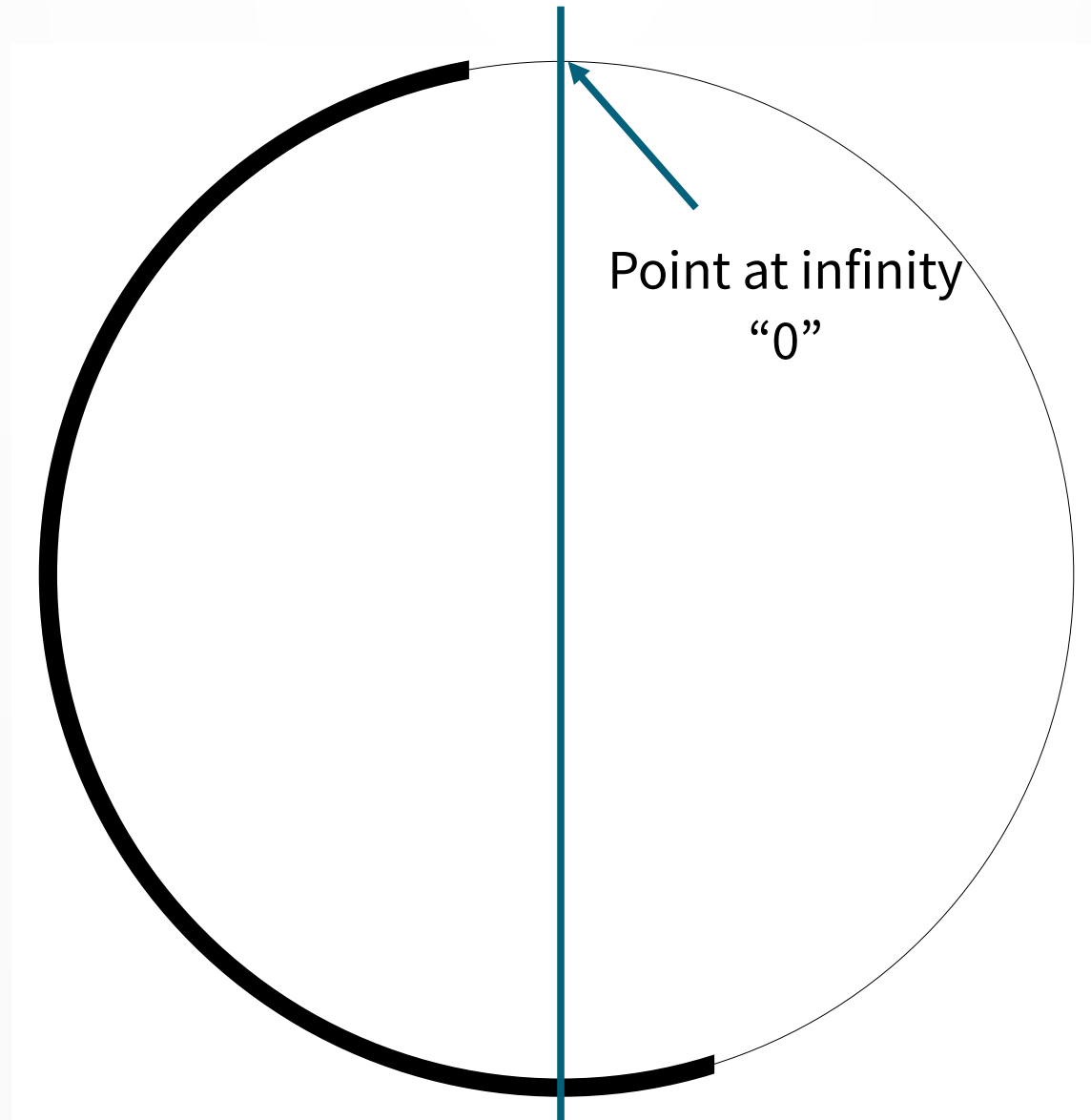
# Clamped Scalar Inverse (Curve25519)

- Prime sub group
  - $L = 2^{252} + 0x14def9dea2f79cd65812631a5cf5d3ed$
- Normal scalar inverse
  - $\text{ScalarInverse} = \text{power\_mod}(\text{Scalar}, L - 2, L)$

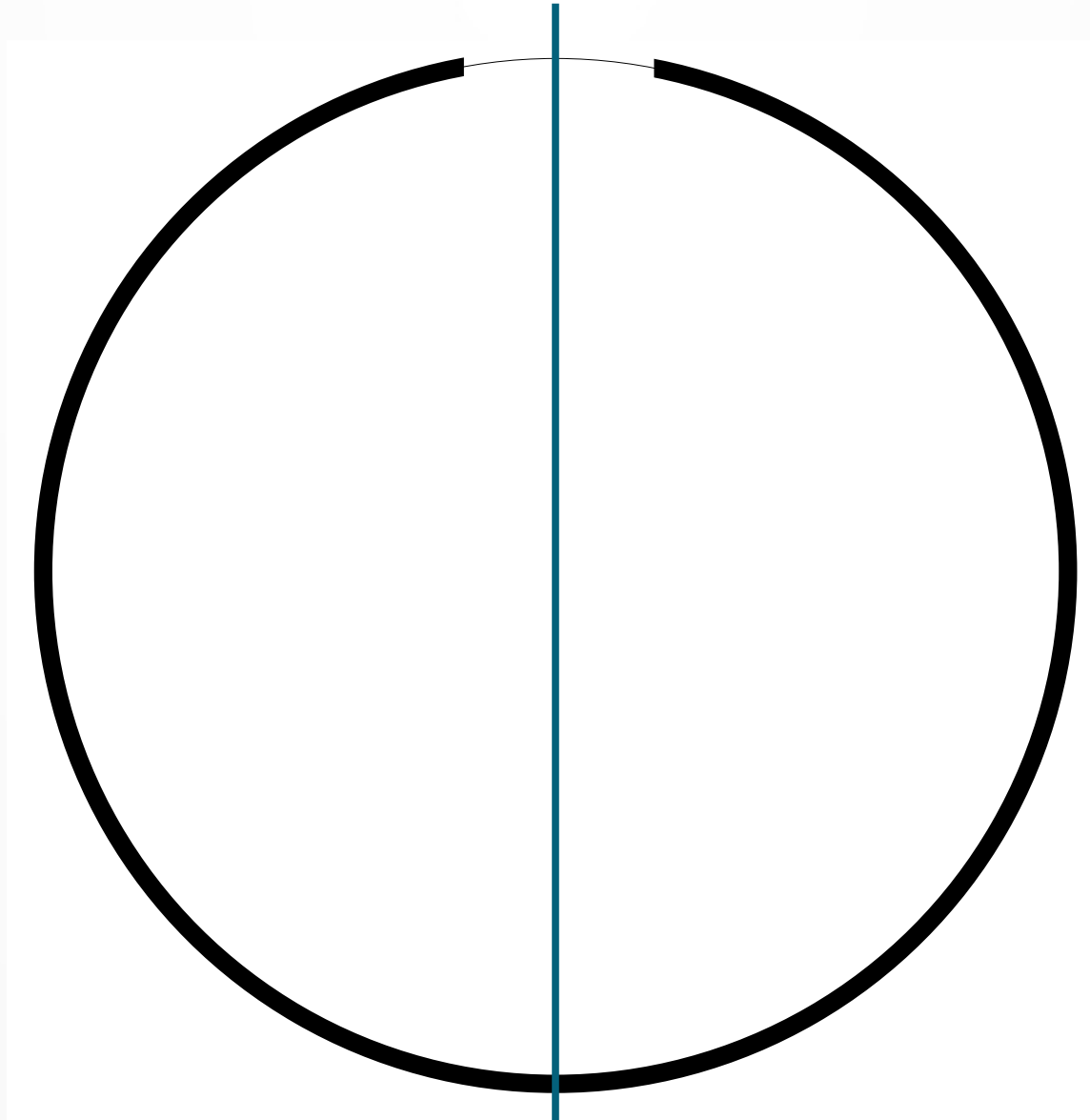
# Clamped Scalar Inverse (Curve25519)

- Prime sub group
  - $L = 2^{252} + 0x14def9dea2f79cd65812631a5cf5d3ed$
- $\text{ScalarInverse1} = \text{power\_mod}(\text{Scalar}, L - 2, 8 * L)$
- $\text{ScalarInverse2} = 8 * L - \text{ScalarInverse1}$
- $\text{checkBit}(\text{ScalarInverse1}, 254) \neq 0$ 
  - $\text{ScalarInverse1}$
  - Otherwise  $\text{ScalarInverse2}$

# Clamped Scalar Inverse Failure



# Clamped Scalar Inverse Failure



# Clear the Cofactor (Curve25519)

- Prime sub group
  - $L = 2^{252} + 0x14def9dea2f79cd65812631a5cf5d3ed$
- Multiply scalar by “inverse of 8 multiplied 8”
  - That’s “8/8” which is “1”
- $\text{Clear} = \text{power\_mod}(8, L - 2, L) * 8$
- $\text{NewScalar} = \text{Clear} * \text{Scalar} \pmod{8 * L}$



# “Myth #9”

- OPAQUE's Footgun

# “Myth #9”

- I found one in the wild
- They now wrap ChaChaPoly1305 with HMAC-SHA512

# Cheat Sheet

- Balanced
  - CPace
- Augmented
  - BS-SPEKE
- Doubly Augmented
  - Double BS-SPEKE
- Identity
  - CHIP
- Balanced PAKEs don't need key stretching
- bscrypt (minimums)
  - $m=256$  (256 KiB),  $t=8$ ,  $p=1$
  - $m=256$  (256 KiB),  $t=4$ ,  $p=2$
  - $m=256$  (256 KiB),  $t=3$ ,  $p=3$
  - General
    - $m$ =highest per core cache level in KiB
    - $t \geq \max(2, 1900000/1024/m/p)$
    - $p \leq \text{cores}$

# What is bcrypt?

- See BSidesLV 2022 (PasswordsCon track)
  - “bcrypt – A Cache Hard Password Hash”

# Minimum Password Settings

<https://tobtu.com/minimum-password-settings/>

# Questions?

- Twitter: @Sc00bzT
- Github: Sc00bz
- steve at tobtu.com

# References

- [1] Send files <https://github.com/magic-wormhole>
- [2] Phone spoofing <https://commsrisk.com/?p=35506>
- [3] SPEKE <https://jablon.org/jab96.pdf> / <https://jablon.org/jab97.pdf>
- [4] Doubly Augmented <https://moderncrypto.org/mail-archive/curves/2015/000424.html>
- [5] (strong) AuCPace <https://ia.cr/2018/286>
- [6] OPAQUE <https://ia.cr/2018/163>
- [7] CHIP, CRISP <https://ia.cr/2020/529>
- [8] EKE <https://www.cs.columbia.edu/~smb/papers/neke.pdf>
- [9] OPAQUE's footgun <https://ia.cr/2020/1491>



# Bonus Slides

- bscrypt
- BS-SPEKE secure registration

# bscrypt

- The fun slides from my BSidesLV 2022 talk
- But first one info slide

# Accumulators

```
R ^= sbox0[L >> 32 & mask];
```

```
R += sbox1[L & mask];
```

```
L ^= sbox0[R >> 32 & mask];
```

```
L += sbox1[R & mask];
```

```
...
```

# Overlapping S-boxes

S0



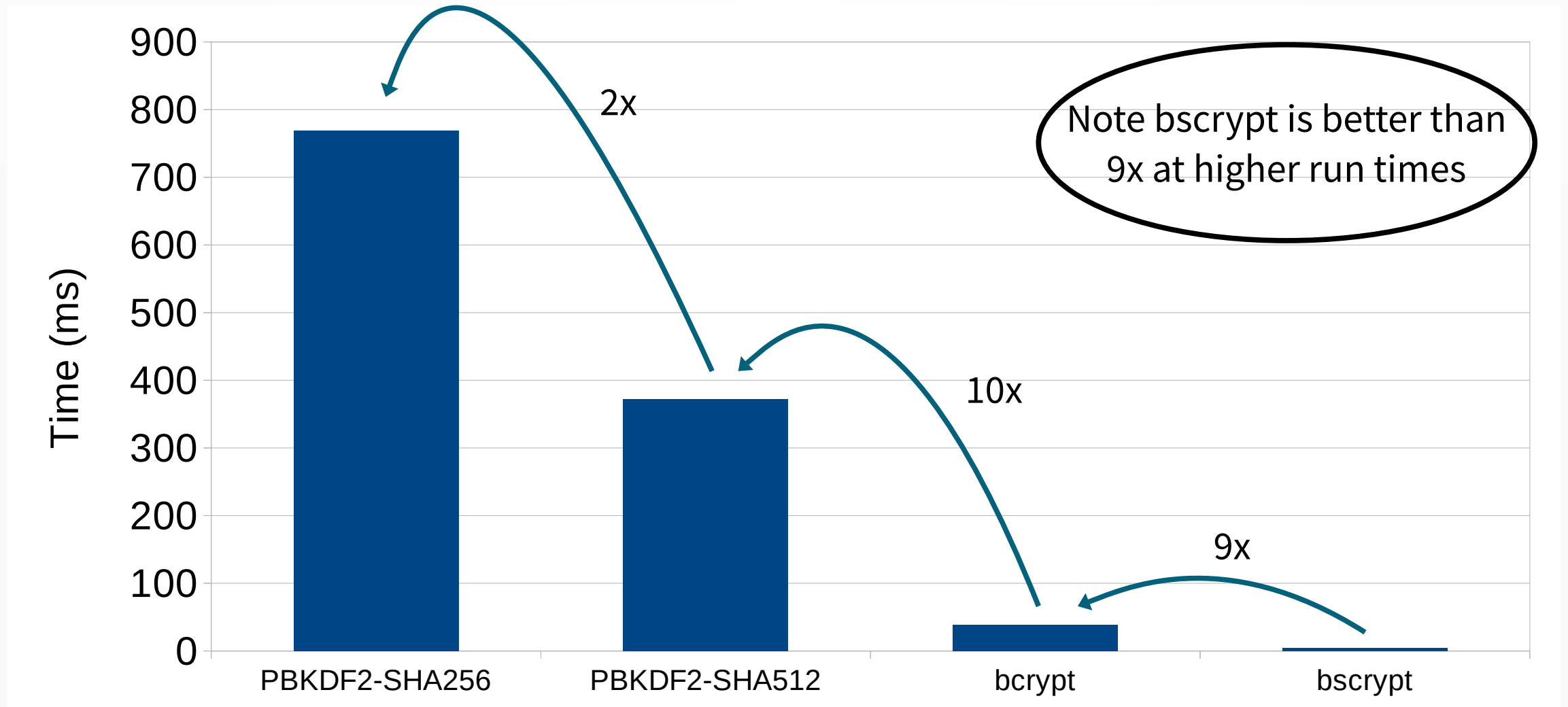
S1

S0



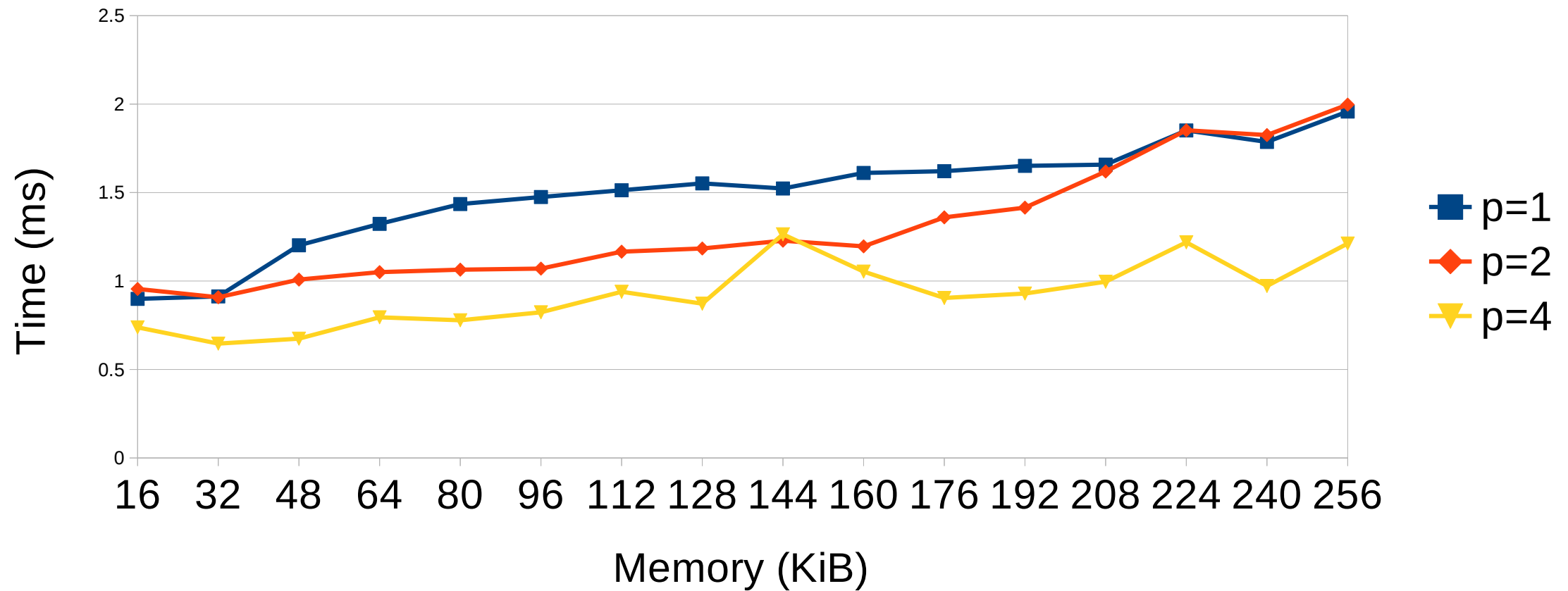
S1

# i5-6200U: Settings for ~5300 KH/s/GPU



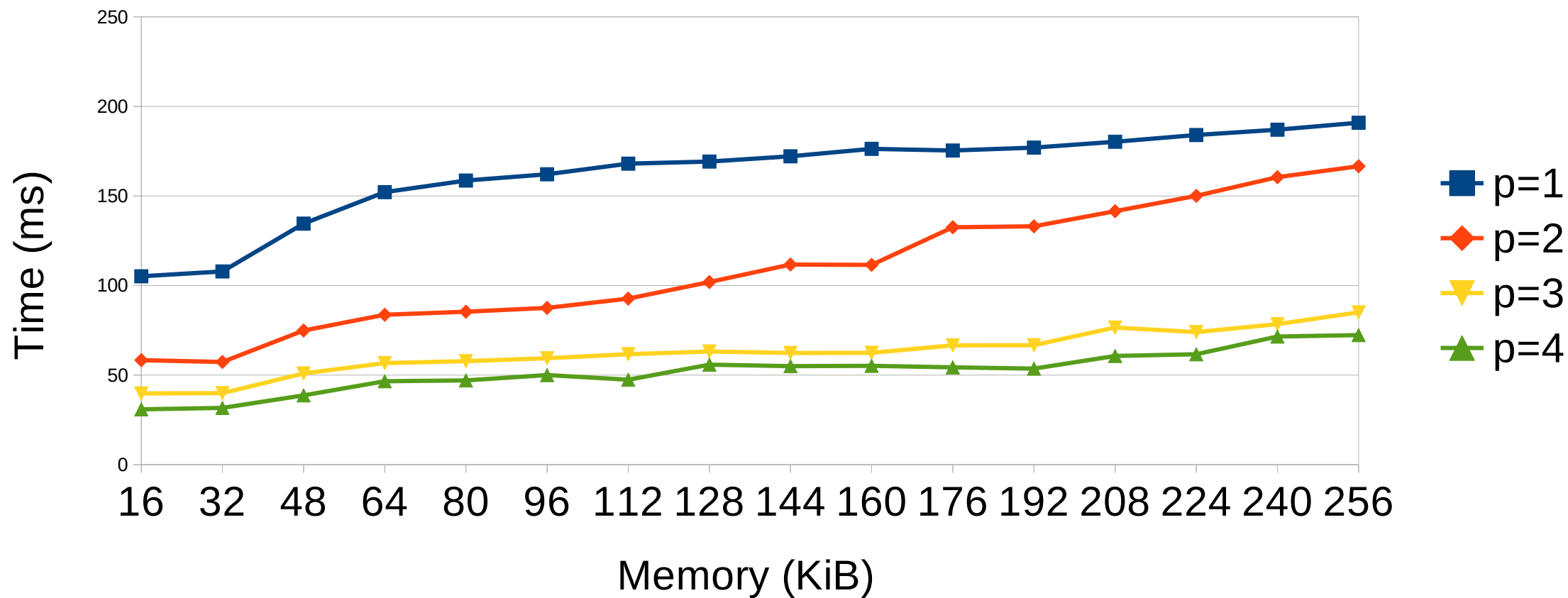
# i5-6500: 32 KiB L1, 256 KiB L2, 6 MiB L3

Settings for <10 kH/s/GPU



# i5-6500: 32 KiB L1, 256 KiB L2, 6 MiB L3

Settings for <85 H/s/GPU (equivalent to bcrypt cost 15)





# BS-SPEKE Secure Registration

S: Check client verifier

S: verifierS = H(...)

S: sessionKey = H(...)

S: encReg = aead\_encrypt(sessionKey, reg || regMac)

C←S: verifierS, encReg

C: Check server verifier

C: sessionKey = H(...)

C: reg || regMac = aead\_decrypt(sessionKey, encReg)

C: Checks regMac == MAC(macKey, reg \* G)